

MATH COUNTY INVITATIONAL **MATH TOURNAMENT** FOR GRADES 4-6

Some Problems From 2008

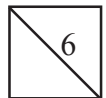
2008 Individual Event

2. What missing number makes the statement true? $44 \times 32 = 64 \times \square$
6. The area of a square is less than 200 sq cm. The length in centimeters of each side is a counting number. What is the greatest perimeter that the square can have, in cm?
9. Amy plays Zane in a game with twelve rounds. In each round, the winner scores 5 points and the loser scores 3 points. At the end of the game, Zane's total score is 44 points. How many rounds did Amy win?

The individual event contained 10 problems.

2008 Team Event

11. Find the value: $(6 - 12) \times (6 - 9) \times (6 - 6) \times (6 - 3)$.
15. What missing number makes the statement true? $\frac{3}{5} + 17 = \frac{\square}{15} + 16$
19. In the square shown, the length of the diagonal is 6 cm. What is the area of the square, in square centimeters?



The team event contained 10 problems.

2008 Tiebreaker Event

21. Brionna walks exactly 5 blocks in 7 minutes and 30 seconds. At this rate, what is the total number of blocks that she walks in 12 minutes?

5 problems are provided to break ties.

MATH COUNTY INVITATIONAL MATH TOURNAMENT FOR GRADES 4-6

Sample Solutions

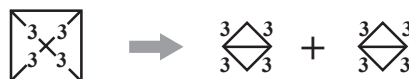
2008 Individual Event

2. **22** Doubling the 32 and halving the 44 does not change the product, nor does switching the positions of two numbers multiplying each other.
6. **56** Since $10^2 = 100$ and $20^2 = 400$, the side-length of the square is between 10 and 20. The side-length is less than 15 cm because $15^2 = 225$. The area of the square is $14^2 = 196$, the side-length is 14 cm and the perimeter is 56 cm.
9. **8** **METHOD 1:** Think of the scoring this way: each player gets 3 points per round just for playing and the winner of the round receives a bonus of 2 points. If we remove those 3 points per round from each person, then the only scoring is 2 points per round for the winner. For the whole game each player would have scored 36 fewer points, so Zane would have scored $44 - 36 = 8$ points. At 2 points per round, he would have won 4 rounds and Amy would have won 8 rounds.

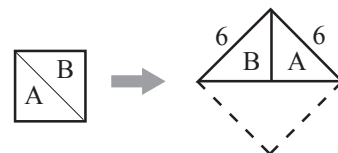
METHOD 2: If Zane won every round, the final score would have been 60-36 in his favor. Each round he loses lowers his total score by $5 - 3 = 2$ points. However, his total score was 44 points, which is 16 points less than 60 points. He lost (and Amy won) $16 \div 2 = 8$ rounds.

2008 Team Event

11. **0** In the third set of parentheses, the value is 0. The product of 0 and any number is 0.
15. **24** $\frac{\square}{15} + 16$: $\frac{3}{5} + 17 = \frac{9}{15} + 17 = \frac{9}{15} + (\frac{15}{15} + 16) = (\frac{9}{15} + \frac{15}{15}) + 16 = \frac{24}{15} + 16$. The numerator is 24.
19. **18** **METHOD 1:** Draw the other diagonal and move the four triangles as shown to form two small squares. Then the sum of the areas of the two small squares, $9 + 9$, equals the area of the original square, 18 sq cm.



METHOD 2: Rearrange the two given triangles as shown and draw the two dashed lines to complete the square. The area of the square is $6 \times 6 = 36$ sq cm. The area of the original square is equal to the upper half of the diagram, 18 sq cm.



2008 Tiebreaker Event

- T1. **8** At that rate she walks 10 blocks in 15 minutes, which is 2 blocks every 3 minutes. Thus in $12 = 4 \times 3$ minutes, she walks $4 \times 2 = 8$ blocks.